## OPERATIONS RESEARCH

Paper-ME-406E
Time Allowed : 3 Hours] [Maximum Marks : 100
Note : Attempt five questions in all, selecting at least one question from each Unit.

## UNIT-I

1. A firm manufactures pain relieving pills in two sizes A and B. Size A contains 4 grains of element X, 7 grains of element $Y$ and 2 grains of element $Z$. Size B contains 2 grains of element X, 10 grains of element Y and 8 grains of element Z. It is found by users that it requires at least 12 grains of element $\mathrm{X}, 74$ grains of element Y and 24 grains of element Z to provide immediate relief. It is required to determine the least number of pills a patient should take to get immediate relief. Formulate the problem as Standard linear programming problem. 20
2. Compute the optimal solutions to the L.P. problem : 20

Maximize : $\mathrm{Z}=2 \mathrm{x}_{1}-4 \mathrm{x}_{2}+5 \mathrm{x}_{3}-6 \mathrm{x}_{4}$
Subject to the constraints : $\mathrm{x}_{1}+4 \mathrm{x}_{2}-2 \mathrm{x}_{3}+8 \mathrm{x}_{4} \leq 2$

$$
\begin{aligned}
& -x_{1}+2 x_{2}+3 x_{3}-4 x_{4} \leq 1 \\
& x_{1}, x_{2}, x_{3}, \quad x_{4} \geq 0
\end{aligned}
$$

## UNIT-II

3. Find the Optimal solution to the Transportation problem in which the cell contains the transportation cost in Rupees : 20 W1 W2 W3 W4 W5 Available

| F1 | 7 | 6 | 4 | 5 | 9 | 40 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| F2 | 8 | 5 | 6 | 7 | 8 | 30 |
| F3 | 6 | 8 | 9 | 6 | 5 | 20 |
| F4 | 5 | 7 | 7 | 8 | 6 | 10 |
| Required | 30 | 30 | 15 | 20 | 5 | 100 |

4. Given below is the information of a project :
Activity
Immediate
Time (days)
Predecessor

| A | - | 3 |
| :---: | :---: | :---: |
| B | - | 4 |
| C | - | 2 |
| D | A,B | 5 |
| E | B | 1 |
| F | B | 3 |
| G | F,C | 6 |
| H | B | 4 |


| Activity | Immediate <br> Predecessor | Time (days) |
| :---: | :---: | :---: |
| I | E,H | 4 |
| J | E,H | 2 |
| K | C,D,F,J | 1 |
| L | K | 5 |

Draw the network and find the Critical path. ..... 20
UNIT-III
5. (a) What is the need of Simulation ? How you can use Monte Carlo simulation for the Industrial applications ? Give examples.10
(b) Ten villages contain 500, 420, 690, 810, 230, 140, 1064, 290, 385 and 680 fields respectively. Make a random selection of 6 fields using Random numbers table. 10
6. A decision problem has been expressed in the following Payoff table :

## Outcomes

| Action | I | II | III |
| :--- | :---: | :---: | :---: |
| A | 10 | 20 | 26 |
| B | 30 | 30 | 60 |
| C | 40 | 30 | 20 |

(a) What is the minimum payoff action ?
(b) What is the minimum opportunity loss action ?

## UNIT-IV

7. Goods trucks arrive randomly at a stockyard with a mean of 8 trucks/hour. A crew of four operatives can unload a truck in 6 minutes. Trucks waiting in queue to be unloaded are paid a waiting charge at the rate of Rs. 60/hour. Operatives are paid a wage rate of Rs. 20/hour. It is possible to augment the crew strength to 2 or 3 (of four operatives per crew) when the unloading time will be 4 minutes 0 $r$
3 minutes respectively per truck. Find the optimal crew size.
8. Find the Optimal strategies of X and Y and the value of the game :

20

|  |  | Y |  |
| :---: | :---: | :---: | :---: |
|  | -6 | 10 | 11 |
| X | -1 | -2 | -3 |
|  | -1 | -2 | -4 |

